

## MAT631 PROBLEM SET 8

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**Instructions.** Please read the instructions on the course website carefully before submitting your solution(s).

### Questions.

(1) (**Shubham**) Prove that

$$s_{1^n} = \sum_{k \geq n} \binom{k-1}{n-1} G_{1^k}.$$

(2) (**Anant**) Prove that

$$g_{1^n} = \sum_{k=1}^n \binom{n-1}{k-1} s_{1^k}.$$

(3) (**Anubhav**) Prove that

$$g_\lambda = \sum_{\mu \subseteq \lambda} f_\lambda^\mu s_\mu.$$

(4) (**Kanak**) Prove the following

(a)  $X_{K_n} = n!e_n.$

(b)  $X_{K_n^c} = e_{1^n} = h_{1^n} = m_{1^n}.$

(c) If  $G_1$  and  $G_2$  are connected components of a graph  $G$  then  $X_{G_1}X_{G_2} = X_G.$