Indian Institute of Information Technology (IIIT) Manipur Re-Assessment I, March 2023

Course Title: Optimization Techniques

Semester: CSE VI

Date of Examination: 10 March 2023

Part A
$$(5 \times 2 \text{ marks} = 10 \text{ marks})$$

Instructions

• All questions are compulsory in this part.

Questions

- 1. Explain what is rank of a matrix with a suitable (non-trivial) example.
- 2. Mention four advantages of the revised simplex method over the usual simplex method.
- 3. Explain what is cycling in the simplex method.
- 4. Define the inverse of a matrix and write a formula of the inverse of a matrix using the cofactors of the matrix.
- 5. If $B_R = \begin{pmatrix} 1 & -c_B^T \\ 0 & B \end{pmatrix}$, then prove that $B_R^{-1} = \begin{pmatrix} 1 & c_B^T B^{-1} \\ 0 & B^{-1} \end{pmatrix}$.

Part B $(3 \times 5 \text{ marks} = 15 \text{ marks})$

Instructions

- Question 6 is compulsory in this part. For questions 7 and 8, you can choose to do either part (a) or part (b).
- If you do both parts for a question then marks will be awarded only for the first answered part (which is not crossed-out), even if the solution is not complete.

Questions

- 6. Verify whether the following problem is unbounded or bounded? Maximize $2x_2 + x_3$ subject to $x_1 - x_2 \le 5, -2x_1 + x_2 \le 3, x_2 - 2x_3 \le 5$ and $x_1, x_2, x_3 \ge 0$.
- 7. (a) Explain mathematically (with all relevant details), the stopping criterion or optimality in the simplex method.

OR

(b) Use the simplex method to determine a solution of the following set of linear equations:

$\begin{aligned} x + y &= 4\\ 2x + y &= 10. \end{aligned}$

Course Code: MA301

Maximum Marks: 25

Time: 60 minutes

8. (a) Solve the following LPP: Maximize $a + 2b + 3c + \dots + 26z$ subject to

$$a + b + \dots + z \le 1$$
$$b + \dots + z \le 2$$
$$\vdots$$
$$z \le 26$$
$$a, b, \dots, z \ge 0.$$

OR

(b) A set S is called convex is for $0 \le \ell \le 1$ and $x, u \in S$, we have $\ell x + (1 - \ell)u \in S$. Prove that, for a standard LPP the feasible region is a convex subset of \mathbb{R}^n .